

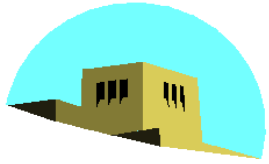


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Texture Mapping

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Objectives

- Introduce Mapping Methods
 - Texture Mapping
 - Environment Mapping
 - Bump Mapping
- Consider basic strategies
 - Forward vs backward mapping
 - Point sampling vs area averaging



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The Limits of Geometric Modeling

- Although graphics cards can render over 10 million polygons per second, that number is insufficient for many phenomena
 - Clouds
 - Grass
 - Terrain
 - Skin



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Modeling an Orange

- Consider the problem of modeling an orange (the fruit)
- Start with an orange-colored sphere
 - Too simple
- Replace sphere with a more complex shape
 - Does not capture surface characteristics (small dimples)
 - Takes too many polygons to model all the dimples



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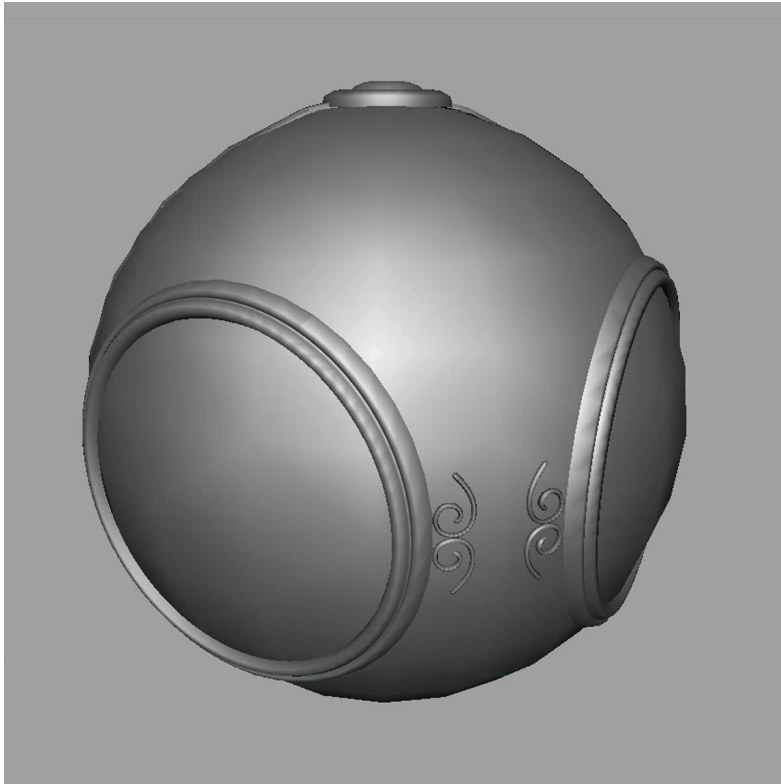
Modeling an Orange (2)

- Take a picture of a real orange, scan it, and “paste” onto simple geometric model
 - This process is known as texture mapping
- Still might not be sufficient because resulting surface will be smooth
 - Need to change local shape
 - Bump mapping



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Texture Mapping



geometric model



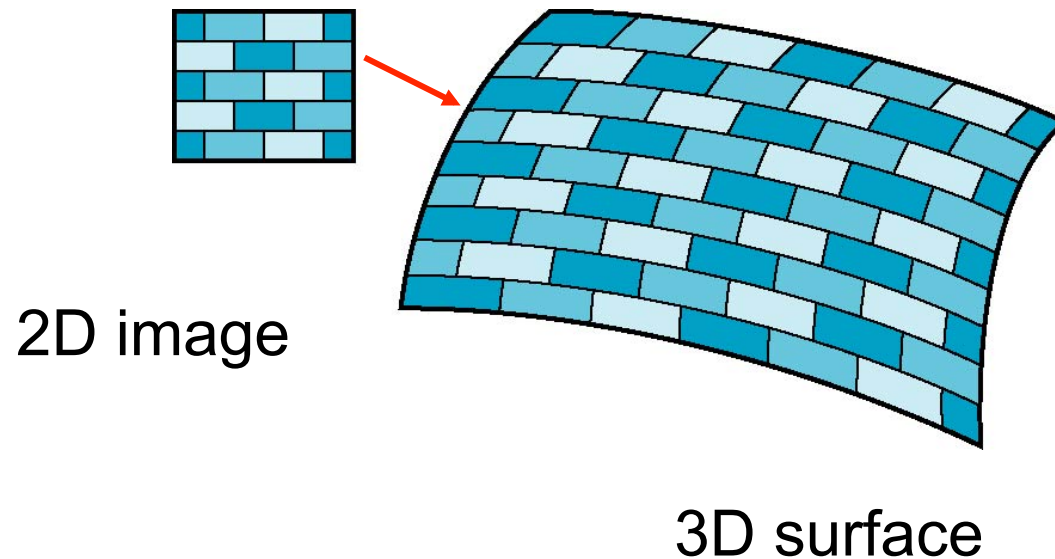
texture mapped



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Is it simple?

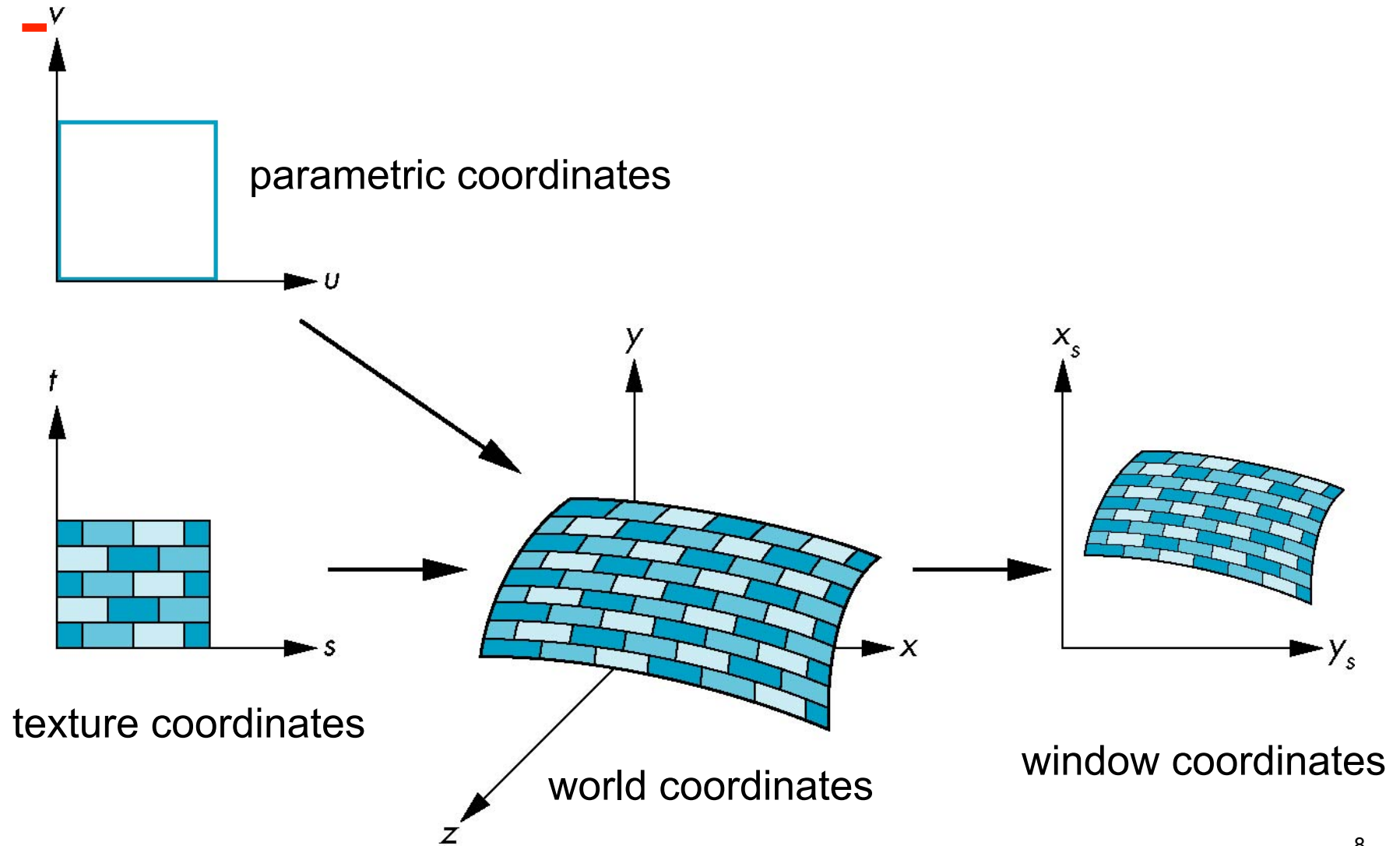
- Although the idea is simple---map an image to a surface---there are 3 or 4 coordinate systems involved





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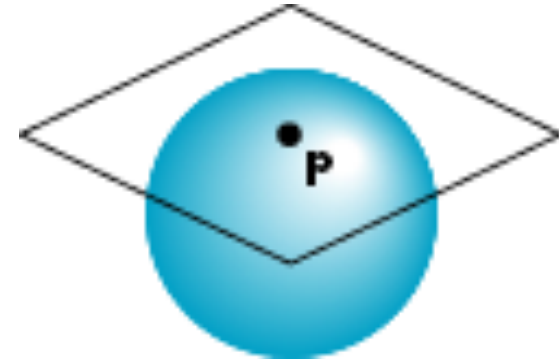
Parametric Form

- For sphere

$$x=x(u,v)=\cos u \sin v$$

$$y=y(u,v)=\cos u \cos v$$

$$z=z(u,v)=\sin u$$



- Tangent plane determined by vectors

$$\frac{\partial \mathbf{p}}{\partial u} = [\frac{\partial x}{\partial u}, \frac{\partial y}{\partial u}, \frac{\partial z}{\partial u}]^T$$

$$\frac{\partial \mathbf{p}}{\partial v} = [\frac{\partial x}{\partial v}, \frac{\partial y}{\partial v}, \frac{\partial z}{\partial v}]^T$$

- Normal given by cross product

$$\mathbf{n} = \frac{\partial \mathbf{p}}{\partial u} \times \frac{\partial \mathbf{p}}{\partial v}$$



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Mapping Functions

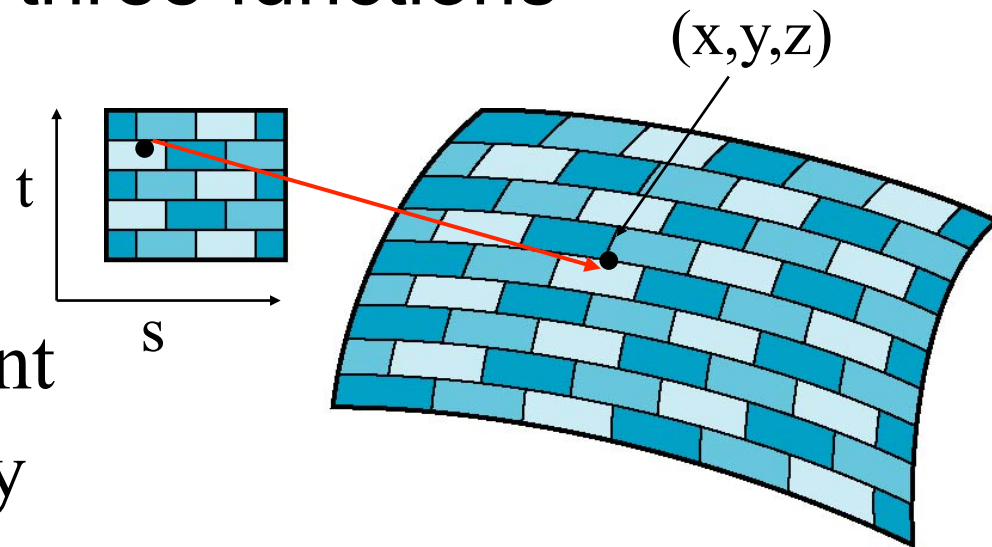
- Basic problem is how to find the maps
- Consider mapping from texture coordinates to a point a surface
- Appear to need three functions

$$x = x(s,t)$$

$$y = y(s,t)$$

$$z = z(s,t)$$

- But we really want to go the other way





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Backward Mapping

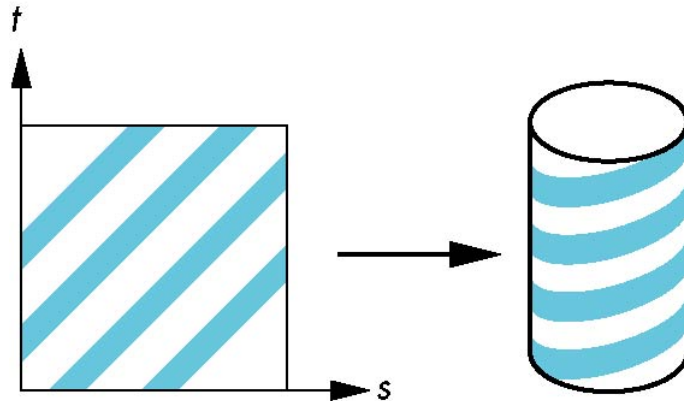
- We really want to go backwards
 - Given a pixel, we want to know to which point on an object it corresponds
 - Given a point on an object, we want to know to which point in the texture it corresponds
- Need a map of the form
$$s = s(x,y,z)$$
$$t = t(x,y,z)$$
- Such functions are difficult to find in general



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Two-part mapping

- One solution to the mapping problem is to first map the texture to a simple intermediate surface
- Example: map to cylinder





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Cylindrical Mapping

parametric cylinder

$$x = r \cos 2\pi u$$

$$y = r \sin 2\pi u$$

$$z = v/h$$

maps rectangle in u,v space to cylinder
of radius r and height h in world coordinates

$$s = u$$

$$t = v$$

maps from texture space



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Spherical Map

We can use a parametric sphere

$$x = r \cos 2\pi u$$

$$y = r \sin 2\pi u \cos 2\pi v$$

$$z = r \sin 2\pi u \sin 2\pi v$$

in a similar manner to the cylinder
but have to decide where to put
the distortion

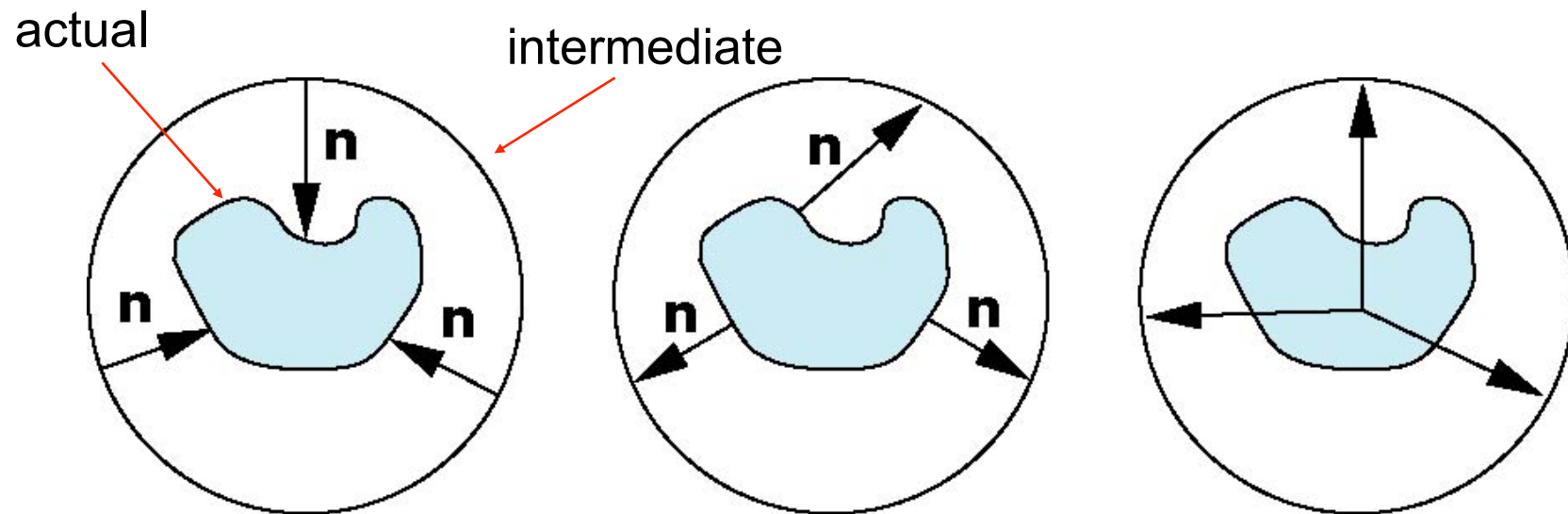
Spheres are used in environmental maps



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Second Mapping

- Map from intermediate object to actual object
 - Normals from intermediate to actual
 - Normals from actual to intermediate
 - Vectors from center of intermediate





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OpenGL Texture Mapping

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Basic Strategy

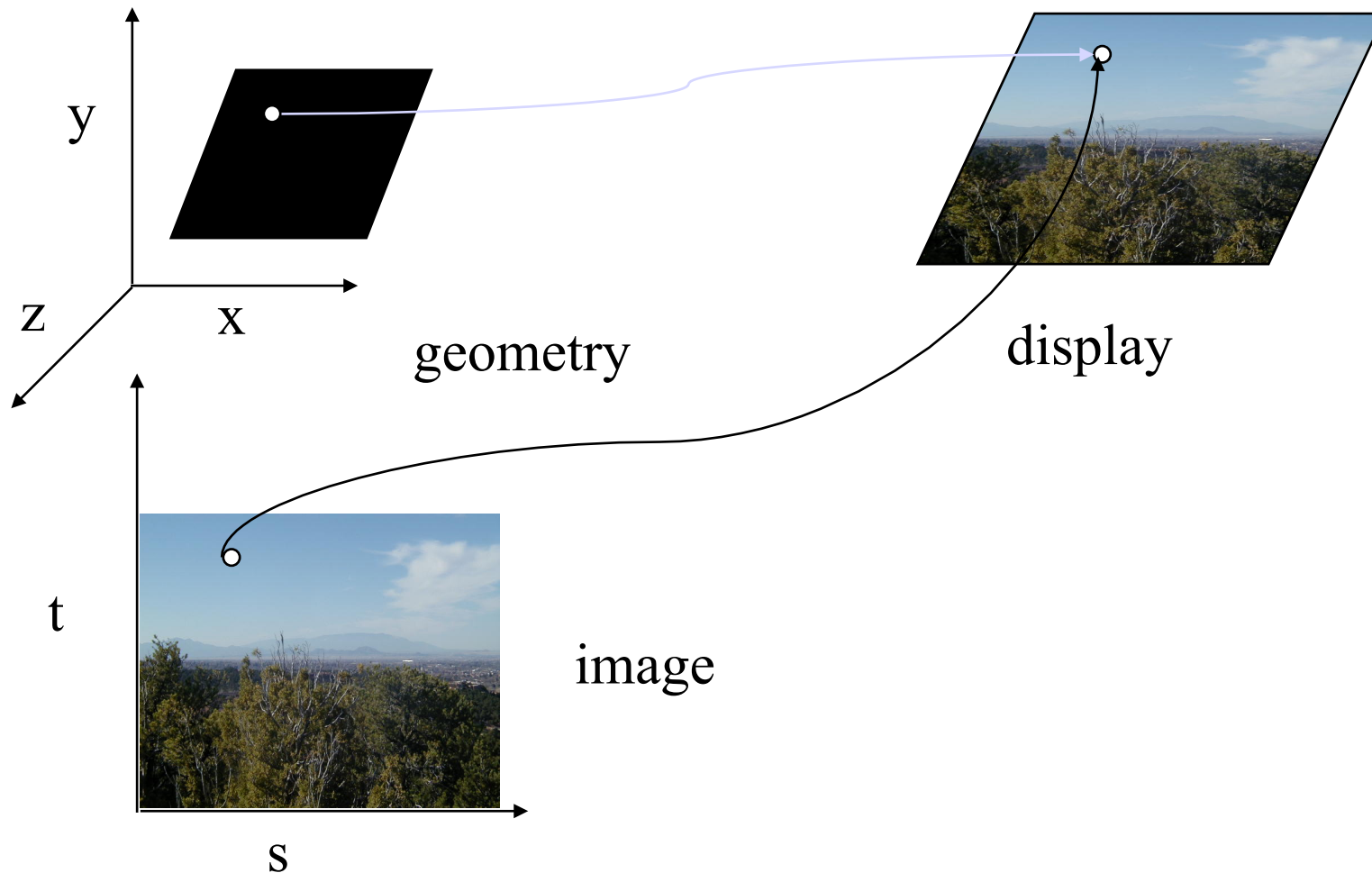
Three steps to applying a texture

1. specify the texture
 - read or generate image
 - assign to texture
 - enable texturing
2. assign texture coordinates to vertices
 - Proper mapping function is left to application
3. specify texture parameters
 - wrapping, filtering



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Texture Mapping

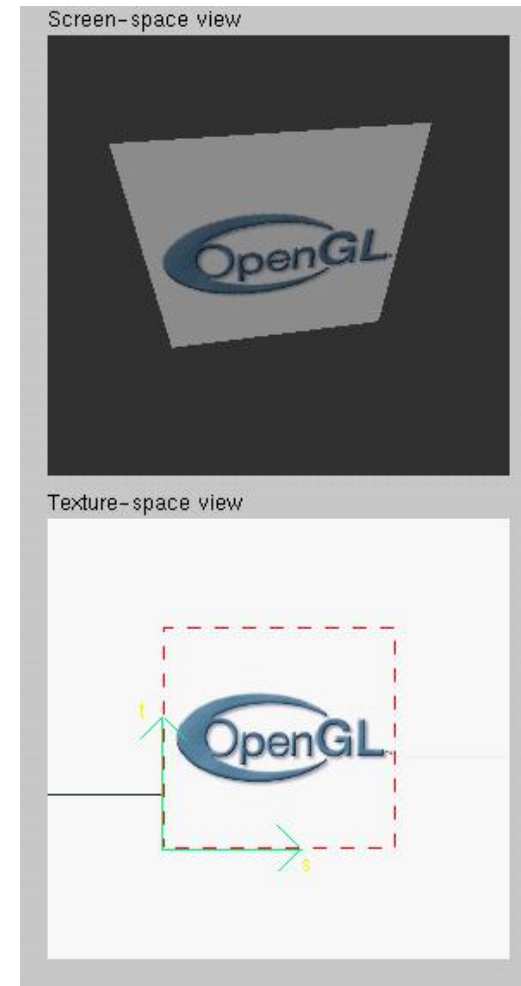




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Texture Example

- The texture (below) is a 256 x 256 image that has been mapped to a rectangular polygon which is viewed in perspective





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Specifying a Texture Image

- Define a texture image from an array of *texels* (texture elements) in CPU memory

```
Glubyte my_texels[512][512];
```

- Define as any other pixel map
 - Scanned image
 - Generate by application code
- Enable texture mapping
 - `glEnable(GL_TEXTURE_2D)`
 - OpenGL supports 1-4 dimensional texture maps



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Define Image as a Texture

```
glTexImage2D( target, level, components,  
             w, h, border, format, type, texels );
```

target: type of texture, e.g. `GL_TEXTURE_2D`

level: used for mipmapping (discussed later)

components: elements per texel

w, h: width and height of `texels` in pixels

border: used for smoothing (discussed later)

format and type: describe texels

texels: pointer to texel array

```
glTexImage2D(GL_TEXTURE_2D, 0, 3, 512, 512, 0,  
            GL_RGB, GL_UNSIGNED_BYTE, my_texels);
```



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Converting A Texture Image

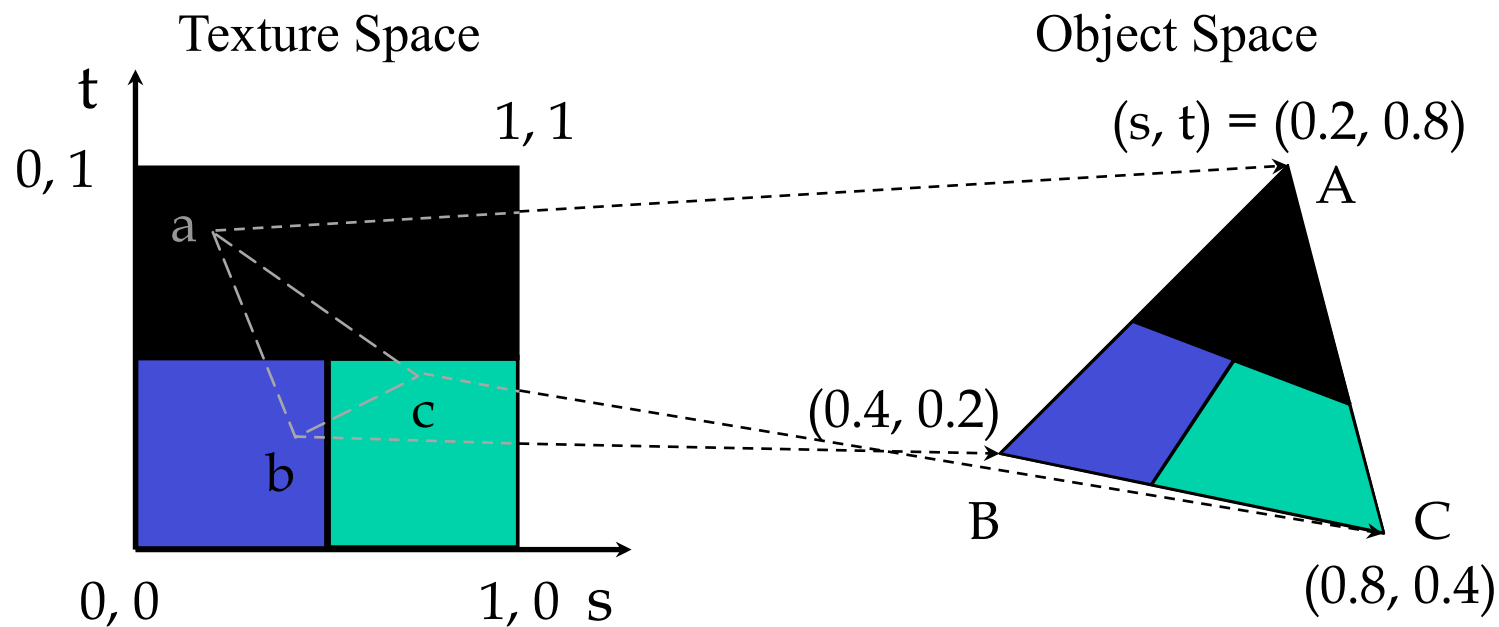
- OpenGL requires texture dimensions to be powers of 2
- If dimensions of image are not powers of 2
 - `gluScaleImage(format, w_in, h_in, type_in, *data_in, w_out, h_out, type_out, *data_out);`
 - `data_in` is source image
 - `data_out` is for destination image
- Image interpolated and filtered during scaling



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Mapping a Texture

- Based on parametric texture coordinates
- `glTexCoord* ()` specified at each vertex





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Typical Code

```
glBegin(GL_POLYGON);  
    glColor3f(r0, g0, b0); //if no shading used  
    glNormal3f(u0, v0, w0); // if shading used  
    glTexCoord2f(s0, t0);  
    glVertex3f(x0, y0, z0);  
    glColor3f(r1, g1, b1);  
    glNormal3f(u1, v1, w1);  
    glTexCoord2f(s1, t1);  
    glVertex3f(x1, y1, z1);  
    .  
    .  
glEnd();
```

Note that we can use vertex arrays to increase efficiency



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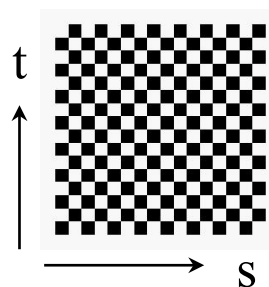
Wrapping Mode

Clamping: if $s, t > 1$ use 1, if $s, t < 0$ use 0

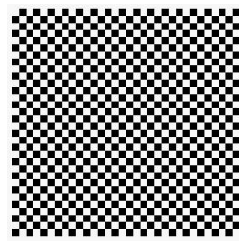
Wrapping: use s, t modulo 1

```
glTexParameteri( GL_TEXTURE_2D,  
                 GL_TEXTURE_WRAP_S, GL_CLAMP )
```

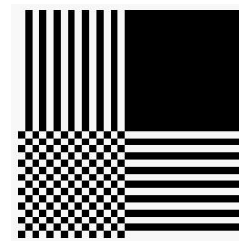
```
glTexParameteri( GL_TEXTURE_2D,  
                 GL_TEXTURE_WRAP_T, GL_REPEAT )
```



texture



GL_REPEAT
wrapping



GL_CLAMP
wrapping